

Recovery from Link Failures in Networks with Arbitrary Topology via Diversity Coding

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Abstract—Link failures in wide area networks are common. To recover from such failures, a number of methods such as SONET rings, protection cycles, and source rerouting have been investigated. Two important considerations in such approaches are the recovery time and the needed spare capacity to complete the recovery. Usually, these techniques attempt to achieve a recovery time less than 50 ms. In this paper we introduce an approach that provides link failure recovery in a hitless manner, or without any appreciable delay. This is achieved by means of a method called diversity coding. We present an algorithm for the design of an overlay network to achieve recovery from single link failures in arbitrary networks via diversity coding. This algorithm is designed to minimize spare capacity for recovery. We compare the recovery time and spare capacity performance of this algorithm against conventional techniques in terms of recovery time, spare capacity, and a joint metric called Quality of Recovery (QoR). QoR incorporates both the spare capacity percentages and worst case recovery times. Based on these results, we conclude that the proposed technique provides much shorter recovery times while achieving similar extra capacity, or better QoR performance overall.

I. INTRODUCTION

Failures in communication networks are common and can result in substantial losses. For example, in the late 1980s, the AT&T telephone network encountered a number of highly publicized failures [1], [2]. In one case, much of the long distance service along the East Coast of the U.S. was disrupted when a construction crew accidentally severed a major fiber optic cable in New Jersey. As a result, 3.5M call attempts were blocked [1]. On another occasion, of the 148M calls placed during the nine-hour-long period of the failure, only half went through, resulting in tens of millions of dollars worth of collateral damage for AT&T as well as many of its major customers [2].

Observing that such wide-scale network failures can have a huge impact, in February 1992, the Federal Communications Commission (FCC) of the U.S. issued an order requesting that carriers report any major outages affecting more than 50K customers lasting for more than 30 minutes. Over a decade, the reports made available to the public showed that network failures are very common and cause significant service interruptions. According to the publicly available data, while most of the reported events impacted up to 250K users, some impacted millions of users [3].

In the early 1990s, AT&T decided to address the restoration problem for its long distance network with an automatic

centrally controlled mesh recovery scheme, called FASTAR, based on digital cross-connect systems [4]. Since then, this subject has seen a significant amount of research. In mesh-based network link failure recovery, the two nodes at the end of the failed link can switch over to spare capacity. Alternatively, all the affected paths could be switched over to spare capacity in a distributed fashion. While the former is faster, the latter will have smaller spare capacity requirement. In this paper, we will use the term source rerouting to refer to mesh-based link or path protection algorithms. In simulations we employ the Simplest Spare Capacity Allocation (SSCA) algorithm [5].

In the mid-1990s, specifications for an automatic protection capability within the Synchronous Optical Networking (SONET) transmission standard were developed. These later became the International Telecommunications Union (ITU) standards G.707 and G.708. The basic idea for protection is to provide 100% redundant capacity on each transmission path through employment of ring structures. SONET can accomplish fast restoration (telephone networks have a goal of restoration within 50 ms after a failure to keep perception of voice quality unchanged by human users) at the expense of a large amount of spare capacity [6], [7]. The restoration times for mesh-based rerouting techniques are typically larger than those of SONET rings, however, the extra transport capacity they require for restoration in the U.S. is generally better than that achievable by SONET rings. In late 1990s, with other major U.S. long distance carriers moving to SONET rings for restoration purposes, an industry-wide debate took place as to whether the mesh-based restoration or the SONET ring-based restoration is better. This debate still continues today. Although most researchers accept that mesh-based restoration may save extra capacity, restoration speeds achievable with mesh-based restoration are generally low and the signaling protocols needed for message feedback are an extra complexity that can also complicate the restoration process.

An extension of the SONET rings is the technique known as p -cycles [8]. In a network, a p -cycle is a ring that goes through all the nodes once. Such a ring will provide protection against any single link failure in the network because there is always an alternative path on the ring that connects the nodes at the end of the failed link, unaffected by the failure. The recovery is carried out by the two nodes that detect the failure at the two ends of the failed link. These nodes reroute the traffic on this link to the corresponding part of the p -cycle. Constructing p -cycles and the corresponding spare capacity

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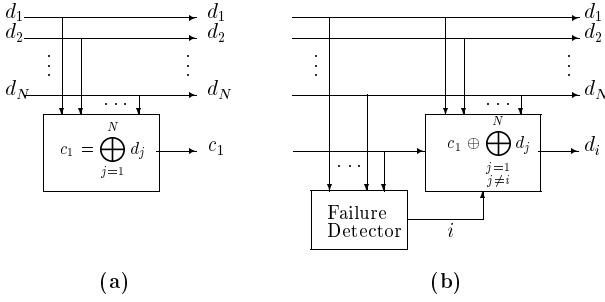


Fig. 1. Diversity coding where N parallel data links are protected against failure by one coded link. (a) Encoder and (b) Decoder.

assignment can be solved by a number of algorithms [8]. Some of these algorithms employ linear programming while there are a number of simpler design algorithms. In this paper, we employ the algorithm in [8, p. 699], which is considered to be within 5% of the optimal solution [8]. We would like to add that in the technique of p -cycles, it is possible to subdivide the network nodes and generate different p -cycle rings for each division separately [8].

Recovery from link failures in IP networks can take a long time [7] because IP routing protocols were not designed to minimize network outages. There has been Internet research that shows a single link failure can cause users to experience outages of several minutes even when the underlying network is highly redundant with plenty of spare bandwidth available and with multiple ways to route around the failure [7]. Needless to say, depending on the application, outages of several minutes are not acceptable, for example, for IP telephony, e-commerce, or telemedicine.

Within the telephony transmission and networking community, hitless restoration from failures is often described as an ideal [8]. Nevertheless, with the methods considered, it could not be achieved because these methods are based on message feedback and rerouting, both of which take time. Whereas, with our method, hitless or near-hitless recovery from single link failures becomes possible given delay buffers that synchronize the paths. This introduces non-appreciable transmission delay. The basic technique is powerful enough that it can be extended to other network failures such as multiple link or node failures.

The concept of a Quality of Recovery (QoR) metric was introduced previously in order to find an overall metric that evaluates the performance of a protection technique and compares it with others, see e.g., [9]. The arguments of the QoR metric depend on the problem and its application. In this paper, we employ a version of the QoR metric from [9] that incorporates spare capacity percentage, restoration time, and data loss.

II. DIVERSITY CODING

The basic idea in diversity coding is given in Fig. 1 [10], [11]. Here, digital links of equal rate d_1, d_2, \dots, d_N are transmitted over disjoint paths to their destination. For the sake of simplicity, assume that these links have a common source and a common destination, and have the same length.

A “parity link” c_1 equal to

$$c_1 = d_1 \oplus d_2 \oplus \dots \oplus d_N = \bigoplus_{j=1}^N d_j$$

is transmitted over another equal length disjoint path. In the case of the failure of link d_i , the receiver can immediately form

$$c_1 \oplus \bigoplus_{\substack{j=1 \\ j \neq i}}^N d_j = d_i \oplus \bigoplus_{\substack{j=1 \\ j \neq i}}^N (d_j \oplus d_j) = d_i$$

since it has $d_1, d_2, \dots, d_{i-1}, d_{i+1}, \dots, d_N$ available and $d_j \oplus d_j = 0$ in modulo-2 arithmetic or logical XOR operation. As a result, d_i is recovered by employing c_1 and $d_1, d_2, \dots, d_{i-1}, d_{i+1}, \dots, d_N$. It is important to recognize that this recovery is accomplished in a feedforward fashion, without any message feedback or rerouting.

We assumed above that the sources and the destinations of $d_1, d_2, \dots, d_N, c_1$ are the same. Diversity coding can actually be extended into network topologies where the source or the destination node is not common. Some examples of such network topologies include multi-point to point, point to multi-point and multi-point to multi-point connections. In some cases, there may be a designated encoding node and a designated decoding node, whereas in some other cases encoding operation can be carried out in source nodes in an incremental fashion. Decoding operation also can be done only at destination nodes, instead of a designated intermediate node. Examples of these topologies can be found in [10], [11], [12].

Diversity coding papers [10], [11] predate the work that relate the multicast information flow in networks to the minimum cut properties of the network [13] by about a decade. This latter work has given rise to the general area of *network coding*. However, in network coding, discovery of optimal techniques to achieve multiple unicast routing in general networks has remained elusive. In this paper, we provide a systematic approach to the related problem of designing an overlay network for link failure recovery in arbitrary networks, based on [10], [11].

As stated above, the main advantage of diversity coding as a recovery technique against failures in networks is the fact that it does not need any feedback messaging. Whereas, mesh-based source rerouting techniques, SONET rings, and the technique of p -cycles do need signaling protocols to complete rerouting. With diversity coding, as soon as the failure is detected, the data can be immediately recovered. As in network coding, this requires synchronization of the coded streams. We refer the reader to [10] for a description of the need for synchronization as well as how to achieve it in diversity coding.

A. Example 1

We will now provide a simple example regarding the use of diversity coding for link failure recovery. Consider the network in Fig. 2(a). This network has a similar topology to the well-known butterfly network commonly used to illustrate the basic

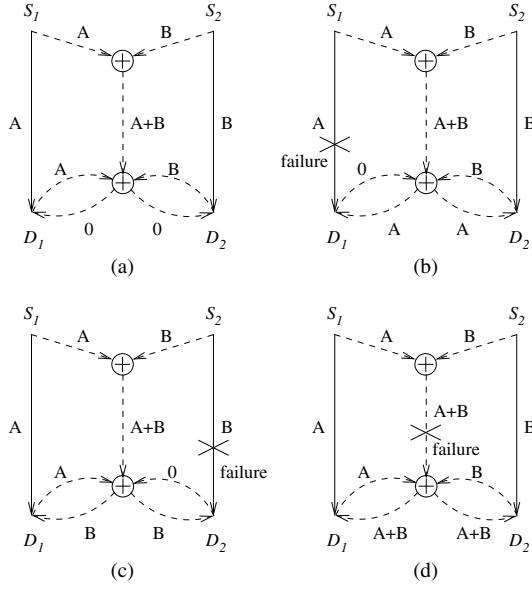


Fig. 2. A simple example for link failure recovery via diversity coding.

concept of multicasting via network coding, first appeared in [13].

In this example, the source node S_1 wishes to transmit its data A to destination node D_1 and the source node S_2 wishes to transmit its data B to destination node D_2 , shown by solid lines. The restoration network is shown via dashed lines. There is an encoder on top which forms $A \oplus B$ which we show as $A+B$. This data is then transmitted to the decoder node. The decoder forms the summation of the data received from the encoder and the two destination nodes. In the case of failures, some of these data will not be present. However, the network is designed such that the destination node will automatically receive the missing data from the restoration network in an automatic fashion. In this example, the central decoder does not carry out any failure detection. This task is carried out by the destination nodes D_1 and D_2 as described below.

In the case of regular operation, the destination nodes receive their data from their data links and receive "0" from the restoration network, as shown in Fig. 2(a). Assume the link from S_1 to D_1 carrying data A failed. In this case, both of the nodes D_1 and D_2 receive data A automatically from the restoration network, as shown in Fig. 2(b). Node D_1 uses this data instead of what it should have been receiving directly from node S_1 . Since node D_2 is receiving its regular data B directly from S_2 , it ignores the data transmitted by the central decoder. The symmetric failure case for the link from S_2 to D_2 is shown in Fig. 2(c). Other failure scenarios will be ignored by D_1 and D_2 since in those cases they receive their data directly from the respective sources S_1 and S_2 . An example of this latter mode of operation is depicted in Fig. 2(d).

B. Example 2

In this example, we will show that diversity coding can result in less spare capacity than source rerouting or p -cycles. Refer to Fig. 3(a). This figure shows the available topology of

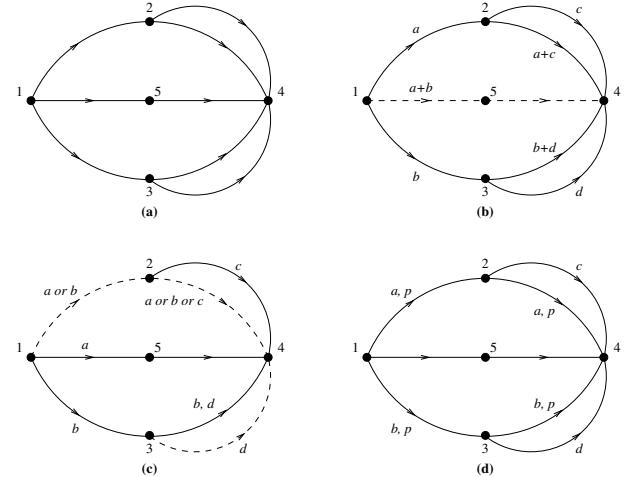


Fig. 3. Spare capacity comparison example.

the network. In this network, each link is bidirectional. There are 4 unit rate flows in the network represented as a, b, c , and d , where a and b are from node 1 to node 4, c is from node 2 to node 4, and d is from node 3 to node 4. The solution for diversity coding is shown in Fig. 3(b). In this solution, path 1-5-4 is a spare link for the protection of either a or b , and it carries modulo-2 sum of a and b . Note that coded signals are not limited to spare links, as the modulo-2 sum of a and c is delivered over the primary path of a . The same applies to the primary path of b . The signals are coded in such a way that node 4 can derive a, b, c , and d given any four of the five incoming links form a full-rank matrix if the remaining link failed. Fig. 3(c) represents the best solution in the case of source rerouting. The upper link is used to protect any failure in transmitting a, b or c . The lower link between nodes 3 and 4 is used to protect flow d . Different from the previous case, we need two unit capacity over the upper link between nodes 3 and 4 due to transmission of b and d separately. The best solution for p -cycles is given in Fig. 3(d). In this solution, there is only one ring that protects every signal. Due to the intermediate node 5, the p -cycles solution cannot offer protection for the path 1-5-4. Protection capacity p , which is unit rate, on the cycle is reserved to carry any failed signal a, b, c , and d since a failure affects at most one of these signals. This guarantees full operation after any failure recovery with an extra cost with respect to diversity coding. Clearly, in this example, both of the approaches of source rerouting and p -cycles result in more spare capacity as compared to the approach of diversity coding.

III. CODING IN NETWORKS WITH ARBITRARY TOPOLOGY

We will now apply the technique described in the previous section to the design of an overlay network for recovery from link failures in arbitrary networks. We approach this problem by examining all possible combinations of standard diversity coding [10], [11], [12]. In doing this, our goal is to come up with a network for which the spare capacity introduced due to diversity coding is minimized. We employ *redundancy*

ratio [12], as the metric that will quantify the efficiency of a particular combination chosen. Redundancy ratio measures the extra capacity introduced in diversity coding. Due to space limitations, we refer the reader to [12] for its definition.

A. Proposed Algorithm

We will now discuss how we utilize the redundancy ratio of each diversity coding combination in designing an efficient diversity coding scheme for a network with arbitrary topology.

The proposed algorithm is intended to search for all possible diversity coding combinations and select those with the smallest redundancy ratio. To that end, we employ a variable called *Threshold*. The threshold begins with a small value (*ThrsdLow*). Diversity coding combinations of N working paths with redundancy ratio values smaller than *Threshold* are accepted, and then *Threshold* is incremented up to its maximum value (*ThrsdHgh*). Within this process, the value N is decremented from a maximum of N_{max} down to 2. The set of unprotected paths is called the *DemandMatrix*, and when N working paths satisfying the redundancy ratio are found, they are taken out of *DemandMatrix*. At the end, a number of paths may remain uncoded. We protect every such path by a dedicated spare path which carries the same data, known as 1+1 APS (Automatic Protection Switch).

A description of the algorithm is given under the heading Algorithm I. In our simulations for this paper, the numerical values used are *ThrsdLow* = 1.6, *ThrsdHgh* = 3.0, and N_{max} = 4.

IV. PERFORMANCE METRICS *SCP*, *RT*, AND *QoR*

There are two dominant factors that specify the performance of a protection technique. These are spare capacity percentage *SCP* and restoration time *RT*. The *QoR* metric combines these quantities into a single one and presents a clearer comparison among restoration techniques. The values of *SCP* are calculated via simulations over sample networks and traffic, which are given in the next section. We employ the following formula for calculating *SCP* in all simulations

$$SCP = \frac{\text{Total Capacity}-\text{Shortest Working Capacity}}{\text{Shortest Working Capacity}}.$$

Shortest Working Capacity is the total capacity when there is no protection and the traffic is routed over shortest paths. The restoration time *RT* is defined as the longest duration that the connection is lost during the recovery process. *RT* is calculated by a modified version of a formula from [14]. For source rerouting, p -cycles, and diversity coding algorithms, the following formulas are used to calculate the restoration time, in respective order

$$RT_{sr} = F + nP + (n + 1) \cdot D + (m + 1) \cdot C + 3 \cdot P + 3 \cdot (m + 1) \cdot D + EP$$

$$RT_{pc} = F + (n + 1) \cdot D + 2 \cdot C + P + EP$$

$$RT_{dc} = F + 2 \cdot D + PD.$$

As in [14], we use F : the time to detect a failure, D : node message processing time, C : time to configure a network

ALGORITHM I: CODE ASSIGNMENT FOR LINK FAILURE RECOVERY VIA DIVERSITY CODING

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for Threshold=ThrsdLow to ThrsdHgh do
  for all combinations of  $N = N_{max}, \dots, 3, 2$  do
    if diversity ratio of combination  $\leq$  Threshold
      then
        if  $flow_1, \dots, flow_K \in DM$  then
          for  $i = 1$  to  $K$  do
            |  $DM = DM - \{flow_i\}$ 
          end
          Update the total, working, and space
          capacities
        end
      end
    end
  end
  for all  $flow_k \in DM$  do
    Apply 1+1 APS protection
     $DM = DM - flow_k$ 
    Update the total, working, and space capacities
  end

```

switch, m : number of hops in the backup route, and n : number of hops from the source node of the failed link to the source. P is the propagation time for the protection path, EP is the propagation time of failure to the closest node and nP is the propagation time until the error signal reaches the source-end node. In addition, PD means propagation delay difference between link-disjoint paths in the diversity coding scheme. As in [15], we set F to 100 μs . Similarly to [14], we set the variable C a number of values, i.e., 500 μs , 1 ms, 5 ms, and 10 ms. The particular form of the *QoR* metric we employ is based on [9]. We define the contributions due to *RT* and *SCP* as

$$Q_{RT} = \frac{1}{1 + 400 \cdot RT^2}, Q_{SCP} = \frac{1}{1 + \left(\frac{SCP}{100}\right)^3}$$

where *RT* is in seconds and the factor 400 accounts for setting $Q_{RT} = 1/2$ for $RT = 50$ ms [9]. Similarly, normalization with 100 is to set $Q_{SCP} = 1/2$ when *SCP* = 100. Finally, we incorporate restoration time, data loss, and spare capacity into the *QoR* metric as

$$QoR = \frac{2 \cdot Q_{RT} + Q_{SCP}}{3}$$

where the factor 2 accounts for both restoration time and data loss, which is proportional to *RT* [9].

V. SIMULATION RESULTS

In this section, we will present simulation results for link recovery techniques previously discussed, in terms of their spare capacity requirements and their restoration times.

The first network studied is the European COST 239 network whose topology is given in Figure 4 [16]. In this graph

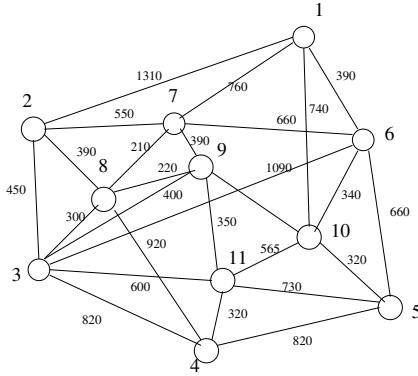


Fig. 4. European COST 239 network. Distances are in km.

TABLE I
COST 239 NETWORK

COST 239 Network, 11 nodes, 26 spans				
Scheme	SCP	RT for different C values (ms)		
		0.5ms	1ms	5ms
Div. Coding	98%	4.8	4.8	4.8
Source Rerout.	90%	39.8	41.8	57.8
p-cycles	64%	26.1	27.1	35.1
				45.1

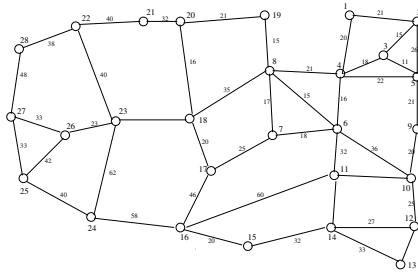


Fig. 5. U.S. long distance network. Distances are in tens of miles.

as well as the others in the sequel, the numbers associated with the nodes represent a node index, while the numbers associated with the edges correspond to the distance associated with the edge. The traffic demand is adopted from [16] and applied to the simulation. This network was previously studied in the context of link failure recovery [8]. We provide SCP and RT results for the three schemes in Table I.

The second network is based on the U.S. long-haul optical network. The topology of this network is shown in Figure 5. It is based on the topology given in [5]. In order to calculate the traffic, we employed a gravity-based model [17] and assumed the traffic between two nodes is directly proportional to the product of the populations of the locations represented by these nodes. Values of SCP and RT for this network are given in Table II.

The third network is one that favors diversity coding over the other two approaches in terms of spare capacity. We came up with this network in order to provide a different example than the two previous networks. The topology of this network is given in Fig. 6. The demand in this network is set such that it is symmetric and most of it originates from and terminates at the two end nodes 1 and 9 [12]. The values of SCP and

TABLE II
U.S. LONG DISTANCE NETWORK

Scheme	SCP	US Long Distance Network, 28 nodes, 45 spans			
		0.5ms	1ms	5ms	10ms
Div. Coding	106%	9.5	9.5	9.5	9.5
Source Rerout.	91%	79.7	83.7	115.7	155.7
p-cycles	107%	59.6	60.6	68.6	78.6

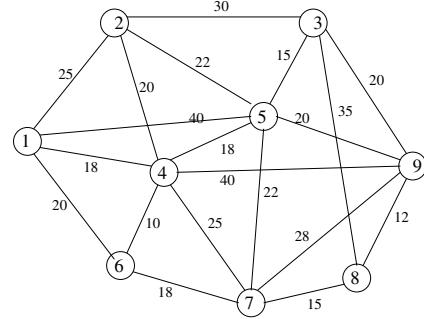


Fig. 6. Synthetic network. Distances are in miles.

TABLE III
SYNTHETIC NETWORK

Scheme	SCP	Synthetic Network, 9 nodes, 20 spans			
		0.5ms	1ms	5ms	10ms
Div. Coding	81%	0.9	0.9	0.9	0.9
Source Rerout.	100%	5.7	8.2	28.2	53.2
p-cycles	85%	2.8	3.8	11.8	21.8

RT are provided in Table III. For this network, the best spare capacity results are obtained by employing the diversity coding approach, similarly to the case we showed in the example in Section II.B.

Comparing the values of SCP for the three networks in Tables I-III, we observe that the three techniques achieve all possible SCP performance orderings, from number one to number three. On the other hand, in terms of the RT performance, the proposed technique is always substantially better. As can be observed, the improvement in RT performance can be close to or even more than an order of magnitude. It is worthwhile to observe that for the U.S. Long Distance network, the RT values with source rerouting or p-cycles are above the critical threshold of 50 ms for all values of C, the network switch reconfiguration time. For this network, values of RT are well below the 50 ms threshold when diversity coding is employed. We would like to note that RT values for diversity coding can be reduced even further. Recall that $RT_{dc} = F + 2 \cdot D + PD$. PD becomes equal to zero if there is one destination node and delay equalization is performed. In this case, RT will become very small, about 300 μ s, making the diversity coding alternative nearly hitless.

As discussed earlier, it is possible to combine RT and SCP into a single metric QoR. Fig. 7 shows values of QoR for the three networks. The results show that QoR for diversity coding is better than the other techniques for all of the networks and

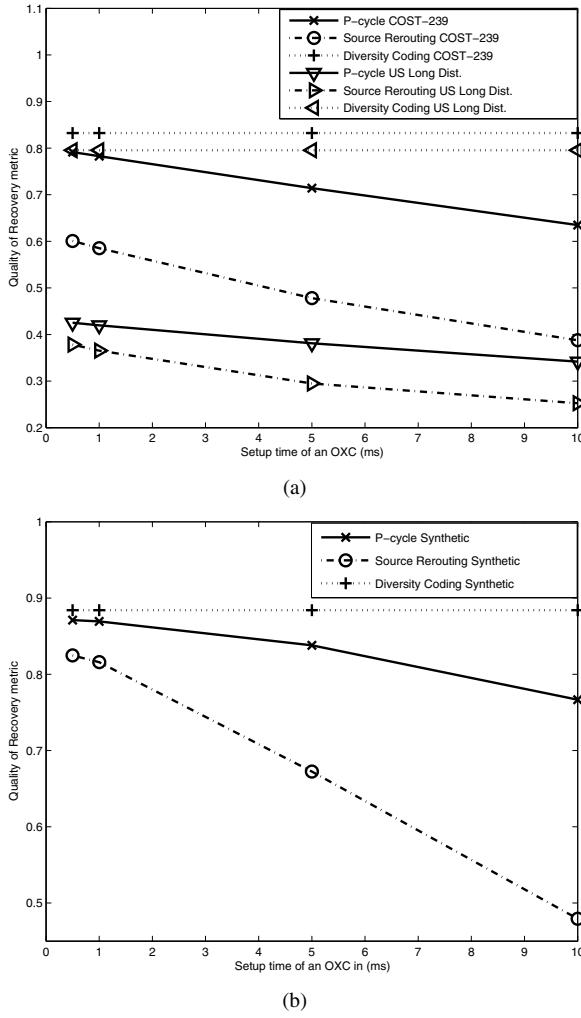


Fig. 7. Quality of Recovery metric results for all three techniques (a) COST 239 and U.S. Long Distance network (b) Synthetic network.

for all possible values of the variable C . Note that while the QoR performance of source rerouting and p -cycles become worse as C increases, that of diversity coding is independent of C , because there is no rerouting involved.

VI. CONCLUSION

In this paper, we employed the technique of diversity coding for providing a single link failure recovery technique in networks with arbitrary topologies. This is accomplished by finding groups of links that can be combined in basic diversity coding topologies, or in other words, mapping the arbitrary topology into efficient groups of basic diversity coding topologies. This approach results in link failure restoration schemes that do not require message feedback or rerouting and therefore are extremely efficient in terms of their restoration speed as shown via realistic calculations. Erasure coding techniques can be employed to extend this technique to recovery from more than one link and node failures.

We emphasize that although synchronization buffering and XOR operation can increase node processing time in diversity coding, these are negligible compared to the propagation delay

and cross-connect configuration time.

We would like to note that a number of recent publications discuss a network coding based link recovery technique [18], [19], similar to diversity coding [10], [11], where advantages of this technique over 1+1 APS in networks are illustrated. It should be noted that, unlike the source rerouting an p -cycles techniques, 1+1 APS is not considered a network restoration technique because it is quite clear that 1+1 restoration is highly inefficient for SCP . The comparison of a technique such as diversity coding for network restoration should be made against techniques such as source rerouting or p -cycles, as carried out in this paper.

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